

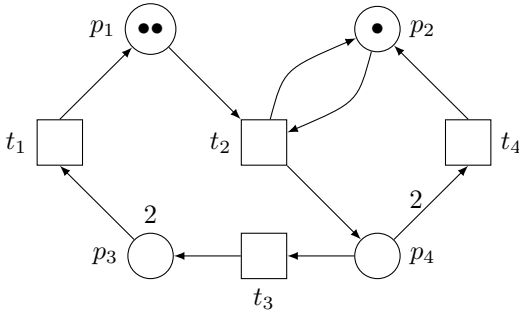
# Networks and Processes

– Written Exam –

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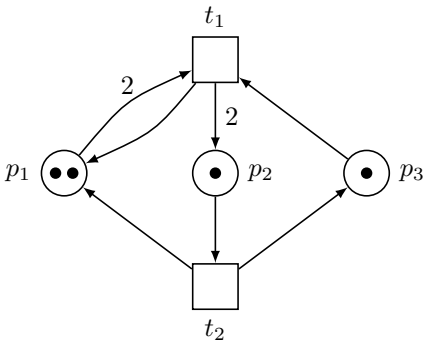
05.02.2009

1. Consider the following P/T net  $N$  with capacities:



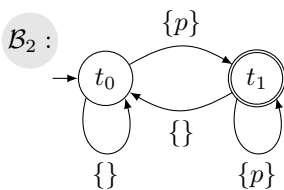
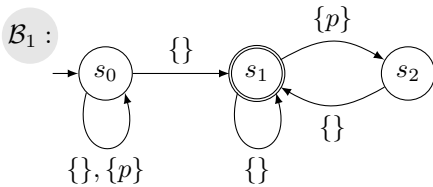
- (a) Construct a P/T net  $N'$  without capacities that is equivalent to  $N$ . Use the construction given in the lectures. (2p)
- (b) Give the largest set of concurrently enabled transitions of  $N'$  in the marking  $M$ , where  $M$  is obtained by firing  $t_2$  in the initial marking. (2p)
- (c) Draw the reachability graph of  $N'$ . (3p)
- (d) Is  $N'$  deadlock-free? If not, indicate the marking(s) in which a deadlock occurs. (1p)
- (e) Identify two independent transitions in  $N'$ . (1p)
- (f) Give the incidence matrix  $C$  of  $N'$ . (1p)
- (g) Find all proper minimal P-invariants by applying Farkas' algorithm to the incidence matrix  $C$ . (3p)
- (h) Identify a nonempty trap in  $N'$  not including  $p_3$ . (1p)

2. Consider the following P/T net:



- (a) Construct a coverability graph of the net using the method discussed in the lectures. (3p)
- (b) Can one conclude from a coverability graph in general that a given network is deadlock-free? Justify your answer. (2p)

3. Büchi automata



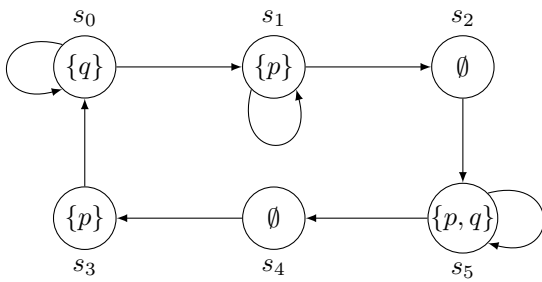
- (a) Consider the Büchi automata  $\mathcal{B}_1$  and  $\mathcal{B}_2$  over the alphabet  $\Sigma = \{\{\}, \{p\}\}$  as shown on the left. Construct an automaton  $\mathcal{B}$  that accepts the intersection of  $\mathcal{L}(\mathcal{B}_1)$  and  $\mathcal{L}(\mathcal{B}_2)$ . Use the method shown in the lectures. (Hint: Consider the reachable states of  $\mathcal{B}$ , only.) (3p)
- (b) Construct in an ad hoc manner a Büchi automaton that is equivalent to  $\mathcal{B}$  but has a smaller number of states. (3p)
- (c) Give two LTL formulas  $\phi$  and  $\psi$  over  $AP = \{p\}$  such that we have  $\mathcal{L}(\phi) = \mathcal{L}(\mathcal{B}_1)$  and  $\mathcal{L}(\psi) = \mathcal{L}(\mathcal{B}_2)$ . (4p)

4. LTL

Consider  $\phi = \mathbf{F}(p \rightarrow q)$ .

- (a) Give  $Sub(\phi)$ . List all elements. (2p)
- (b) Give  $CS(\phi)$ . You may leave out negated formulas. (2p)
- (c) Construct a Büchi automaton  $\mathcal{B}$  over the alphabet  $\Sigma = 2^{\{p,q\}}$  such that  $\mathcal{L}(\mathcal{B}) = \mathcal{L}(\phi)$ . You may use the construction presented in the lectures or give  $\mathcal{B}$  in an ad hoc manner. (2p)

5. CTL



- (a) Consider the Kripke structure on the left, determine the set of states in which the following CTL formulas hold: (3p)
  - i.  $\phi_1 = \mathbf{AF}(p \rightarrow \mathbf{EX} q)$
  - ii.  $\phi_2 = p \mathbf{EU}(\mathbf{AX} q)$
  - iii.  $\phi_3 = \mathbf{EX} \mathbf{AG} p \rightarrow (\mathbf{EX} q)$

- (b) Give a Kripke structure that satisfies  $\mathbf{AG} \mathbf{EX} p \wedge \neg \mathbf{AF} p$ . (2p)